

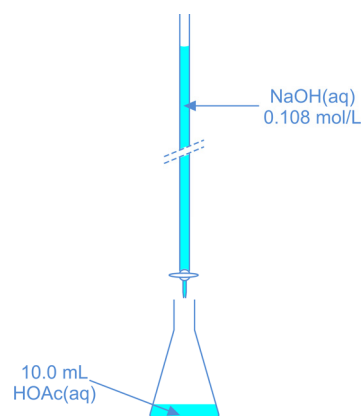
Ionic Equilibriums in Water



#5

Titration of 10.0 mL HOAc-solution (with unknown concentration) with 0.108 mol/L NaOH(aq). The equivalence point is reached after adding 10.4 mL NaOH.

1. Calculate the original HOAc-concentration.
2. Calculate the pH at the start of the titration (0 mL added).
3. Calculate the pH after adding 5.0 mL NaOH.
4. Calculate the pH after adding 10.4 mL NaOH (EP).
5. Calculate the pH after adding 15.0 mL NaOH.



Solutions



1. At the EP the total amount of HOAc has reacted.

10.4 mL 0.108 mol/L NaOH(aq) contains $10.4 \times 10^{-3} \text{ L} \times 0.108 \frac{\text{mol}}{\text{L}} = 1.12 \times 10^{-3} \text{ mol}$ of NaOH.

So the original HOAc-solution also contained $1.12 \times 10^{-3} \text{ mol}$ of HOAc.

The unknown HOAc-concentration was $\frac{1.12 \times 10^{-3} \text{ mol}}{10.0 \times 10^{-3} \text{ L}} = 0.112 \frac{\text{mol}}{\text{L}}$.

2. At the start we have a HOAc-solution 0.112 mol/L.

HOAc is a weak acid, partially reacting with water:



mol/L	HOAc	H ⁺	OAc ⁻
Before reaction	0.112	0	0
Δ	-x	+x	+x
After reaction	0.112 - x	x	x

$$K_{\text{aHOAc}} = \frac{[\text{H}^+] \times [\text{OAc}^-]}{[\text{HOAc}]} = 1.8 \times 10^{-5}$$

$$\frac{x^2}{0.112 - x} = 1.8 \times 10^{-5}$$

$$x^2 + 1.8 \times 10^{-5}x - 2.0 \times 10^{-6} = 0$$

$$x = 0.0014$$

mol/L	HOAc	H ⁺	OAc ⁻
After reaction	0.111	0.0014	0.0014

$$\text{pH} = -\log 0.0014 = 2.85.$$

3. After adding 5.0 mL NaOH, containing $5.0 \times 10^{-3} \text{ L} \times 0.108 \frac{\text{mol}}{\text{L}} = 5.40 \times 10^{-4} \text{ mol}$ of NaOH:

mole	HOAc	NaOH	NaOAc
Before reaction	1.12×10^{-3}	5.40×10^{-4}	0
Δ	-5.40×10^{-4}	-5.40×10^{-4}	$+5.40 \times 10^{-4}$
After reaction	5.80×10^{-4}	0	5.40×10^{-4}

At this moment, we have a buffer solution: HOAc / OAc⁻.

$$\text{pH}_{\text{buffer}} = \text{p}K_{\text{aHOAc}} + \log \frac{[\text{B}]}{[\text{A}]} = 4.75 + \log \frac{\frac{5.40 \times 10^{-4} \text{ mol}}{0.015 \text{ L}}}{\frac{5.80 \times 10^{-4} \text{ mol}}{0.015 \text{ L}}} = 4.72.$$

4. After adding 10.4 mL NaOH (EP), containing $10.4 \times 10^{-3} \text{ L} \times 0.108 \frac{\text{mol}}{\text{L}} = 1.12 \times 10^{-3} \text{ mol}$ of NaOH:

mole	HOAc	NaOH	NaOAc
Before reaction	1.12×10^{-3}	1.12×10^{-3}	0
Δ	-1.12×10^{-3}	-1.12×10^{-3}	$+1.12 \times 10^{-3}$
After reaction	0	0	1.12×10^{-3}

(Na⁺)OAc⁻ (basic salt) reacts partially with water:



mol/L	OAc ⁻	HOAc	OH ⁻
Before reaction	0.0467	0	0
Δ	-x	+x	+x
After reaction	$0.0467 - x$	x	x

$$K_{\text{bOAc}^-} = \frac{[\text{HOAc}] \times [\text{OH}^-]}{[\text{OAc}^-]} = 5.6 \times 10^{-10}$$

$$\frac{x^2}{0.0467 - x} = 5.6 \times 10^{-10}$$

$$x^2 + 5.6 \times 10^{-10}x - 2.6 \times 10^{-11} = 0$$

$$x = 5.1 \times 10^{-6}$$

mol/L	OAc ⁻	HOAc	OH ⁻
After reaction	0.0467	5.1×10^{-6}	5.1×10^{-6}

$$\text{pOH} = -\log 5.1 \times 10^{-6} = 5.29 \Rightarrow \text{pH} = 8.71.$$

5. After adding 15.0 mL NaOH, containing $15.0 \times 10^{-3} \text{ L} \times 0.108 \frac{\text{mol}}{\text{L}} = 1.62 \times 10^{-3} \text{ mol}$ of NaOH:

mole	HOAc	NaOH	NaOAc
Before reaction	1.12×10^{-3}	1.62×10^{-3}	0
Δ	-1.12×10^{-3}	-1.12×10^{-3}	$+1.12 \times 10^{-3}$
After reaction	0	5.00×10^{-4}	1.12×10^{-3}

NaOAc is a weak basic salt and can be neglected.

So the pH is determined by the strong base NaOH: completely dissociated. So the pOH = 1.70 and pH = 12.30.